

Tautological Implications:

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A Proposition  $p$  is set to  $B$  tautological implications if  $p \rightarrow a$  is a tautology.

we denote  $p \rightarrow a$  are  $p \Rightarrow a$  &

1) show that  $(p \rightarrow q) \Rightarrow (\sim q \rightarrow \sim p)$  solution is enough to prove that  $(p \rightarrow q) \Leftrightarrow (\sim q \rightarrow \sim p)$  is a tautology.

$p$	$q$	$p \rightarrow q$	$\sim q$	$\sim p$	$\sim q \rightarrow \sim p$	que
T	T	T	F	F	T	T
T	F	F	T	F	F	T
F	T	T	F	T	T	T
F	F	T	T	T	T	T

Therefore, that  $(p \rightarrow q) \Leftrightarrow (\sim q \rightarrow \sim p)$  is a tautology.

2) Show that the statement is  $(\sim p \wedge \sim q) \rightarrow \sim(p \vee q)$

P	Q	$\sim P$	$\sim Q$	$(\sim p \wedge \sim q)$	$(p \vee q)$	$\sim(p \vee q)$	q
T	T	F	F	F	T	F	T
T	F	F	T	F	T	F	T
F	T	T	F	F	T	F	T
F	F	T	T	T	F	T	T

Therefore, the last column it is clearly that  $(\sim p \wedge \sim q) \rightarrow \sim(p \vee q)$  is a tautology.

3) Show that the statement is

$$(\sim p \vee \sim q) \rightarrow \sim(p \wedge q)$$

P	Q	$\sim P$	$\sim Q$	$(\sim p \vee \sim q)$	$(p \wedge q)$	$\sim(p \wedge q)$	q
T	T	F	F	F	T	F	T
T	F	F	T	T	F	T	T
F	T	T	F	T	F	T	T
F	F	T	T	T	F	T	T

Therefore, the last column is a clearly that  $(\sim p \vee \sim q) \rightarrow \sim(p \wedge q)$  is a.