

Basic logic and proof

logical operation

1) Negation :: \neg or \neg (NOT)

Opposite meaning of the statement

Ex: p: Today is Tuesday

T.P: Today is not Tuesday

Truth table:

(since $p=1$)

P	$\neg P$
T	F
F	T

$$\text{General Formula } \gamma = 2^n - 2^1 = 2$$

2) Conjunction : (AND) (\wedge) cap

If p and q are true other
so it is

Ex: P: surya will go shopping

Q: surya will go Cinema

P/Q: surya will go shopping
and cinema

Truth table:

P	Q	$P \wedge Q$
T	T	T
T	F	F
F	T	F
F	F	F

3) Disjunction or (\vee)

If P or Q is true
otherwise it is false

Ex: 1

P : Suoia will go shopping

Q : Suoia will go cinema

$P \vee Q$: Suoia will go Shopping and
Cinema

$P \vee Q$: True

Truth table

P	Q	$P \vee Q$
T	T	T
T	F	T
F	T	T
F	F	F

Ex: 2

P : Suoia will go shopping

Q : Suoia will not go cinema

$P \vee Q$: Suoia will go Shopping
not cinema.

Ex: 3

P : Suoia will not go shopping

Q : Suoia will go cinema

$P \vee Q$: Suoia will go cinema not
Shopping.

$P \vee Q$: True

Ex: 4

P : Suoia will not go Shopping

Q : Suoia will not go cinema

$P \vee Q$: Suoia will not go Shopping and cinema

$P \vee Q$: False.

4) conditional: (if then) (\rightarrow) implies (con) tense to

If p true and a false
Then $p \rightarrow a$ False,
otherwise it is true.

P	a	$P \rightarrow a$
T	T	T
T	F	F
F	T	T
F	F	T

Ex: 1

P: Gold price is increased

a: sale will be decreased

$P \rightarrow a$: If Gold price is increased
then the sale will be decreased

$P \rightarrow a$: If

$P \rightarrow a$: True

5) Bio conditional: (if and only if) (\leftrightarrow)

The Bioconditional means that both
 $P \rightarrow a$, and $a \rightarrow P$ is true
 $P \leftrightarrow a$ is true
otherwise it is false

P	a	$P \leftrightarrow a$
T	T	T
T	F	F
F	T	F
F	F	T

Ex: 2

P: If I study hard then I will pass

a: And if I pass then I studied hard

$P \leftrightarrow a$: I will pass if and only if
study hard

6) Joint Denial (NOR) (\downarrow)

If both p and q are false, then $p \downarrow q$ is true, otherwise, it is false

p	q	$p \downarrow q$
T	T	F
T	F	F
F	T	F
F	F	T

7) Meet Denial (NAND) (\uparrow)

If both p and q are true then, $p \uparrow q$ is false, otherwise it is true.

p	q	$p \uparrow q$
T	T	F
T	F	T
F	T	T
F	F	T